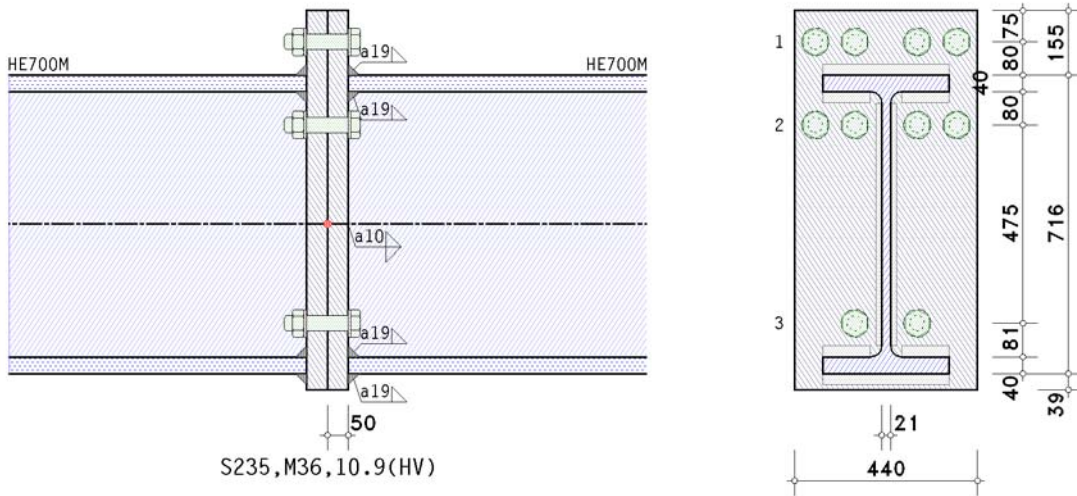
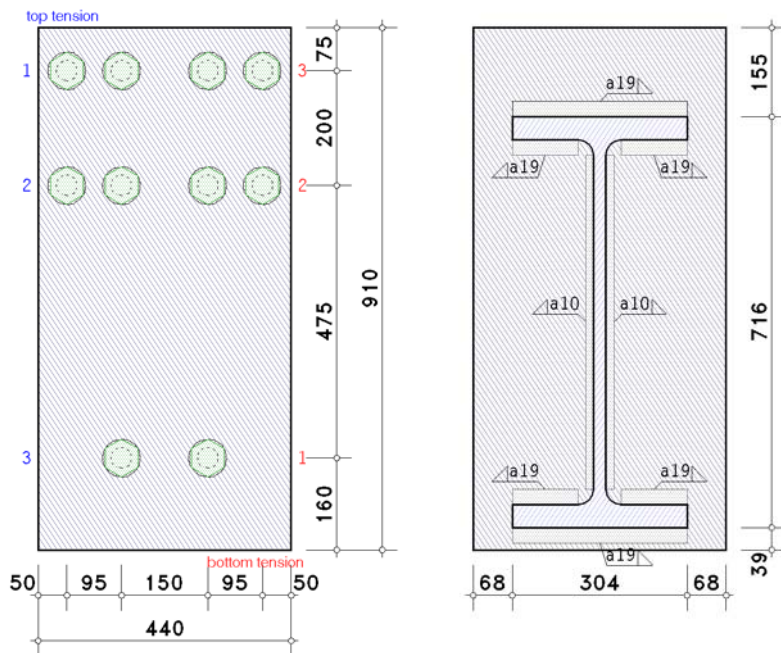


Rigid beam splice EC 3-1-8 (12.10), NA: Deutschland

1. input report



details (section A - A)



steel grade

steel grade S235

bolts

bolt class 10.9, bolt size M36

large wrench size (high strength bolt), preloaded (for info: preloading $F_{p,C^*} = 0.7 \cdot f_{yb} \cdot A_s = 514.7$ kN)

shear plane passes through the unthreaded portion of the bolt

beam parameters

section HE700M

verification parameters

bolted end-plate connection:

thickness $t_p = 50.0$ mm, width $b_p = 440.0$ mm, length $l_p = 910.0$ mm

projections $h_{p,o} = 155.0$ mm, $h_{p,u} = 39.0$ mm

bolts in connection:

3 bolt-rows with 4 bolts (maximum):

row 1: 4 bolts, row 2: 4 bolts, row 3: 2 inner bolts

all bolt-rows considered individually

all bolt-rows for shear transfer (rows 1-3)

verification with der Component method: MNV-interaction acc. to Cerfontaine (in Jaspart/Weynand)

calculation method (4 bolts per row) acc. to the final report of AIF-project 15059

centre distance between outer and inner bolt $w_2 = 95.0$ mm
 centre distance of the bolts to the lateral edge of the end-plate $e_2 = 50.0$ mm
 centre distance of the first bolt-row to the upper edge of the end-plate (end row) $e_o = 75.0$ mm
 centre distance of the last bolt-row to the bottom edge of the end-plate (end row) $e_u = 160.0$ mm
 centre distance of the bolt-rows from each other $p_{1-2} = 200.0$ mm, $p_{2-3} = 475.0$ mm

welds at the connection point:

beam flange top: fillet weld, weld thickness $a = 19.0$ mm
 beam web: fillet weld, weld thickness $a = 10.0$ mm
 beam flange bottom: fillet weld, weld thickness $a = 19.0$ mm

internal forces and moments in the intersection point of system axes

Lk 1: $M_{j,b,Ed} = -2200.00$ kNm $V_{j,b,Ed} = 800.00$ kN

Lk 2: $M_{j,b,Ed} = 650.00$ kNm $V_{j,b,Ed} = 800.00$ kN

Lk 3: $N_{j,b,Ed} = 2100.00$ kN

Lk 4: $N_{j,b,Ed} = -7300.00$ kN

partial safety factors for material

resistance of cross-sections $\gamma_{M0} = 1.00$
 resistance of members in stability failure $\gamma_{M1} = 1.10$
 resistance of bolts, welds, plates in bearing $\gamma_{M2} = 1.25$
 prestressing of high strength bolts $\gamma_{M7} = 1.10$

check of data

ok

utilizations

Lk	$U_{\sigma,b}$	U_{MNV}	U_{ep}	U
1	0.892	0.968	0.331	0.968
2	0.416	0.933	0.331	0.933
3	0.232	0.858	---	0.858
4	0.807	0.996	---	0.996*

$U_{\sigma,b}$: stress utilization at the beam; U_{MNV} : utilization due to MNV-interaction; U_{ep} : utilization due to shear in end-plate

U : utilization of the connection

*) maximum utilization

2. final result

utilization/rotation of the connection

Lk	$S_{j,ini}$ MNm/rad	S_j MNm/rad	φ_j °	U_j	Gleichgewicht			
					ΣH kN	ΣV kN	ΣM kNm	
1	3033.8	3033.8	0.042	0.968	0.00	800.00	2200.00	!!
2	647.9	647.9	0.057	0.933	0.00	800.00	650.00	!!
3	0.0	0.0	0	0.858	2100.00	0.00	0.00	!!
4	0.0	0.0	0	0.996*	7300.00	0.00	0.00	!!

$S_{j,ini}$: initial rotational stiffness; S_j : rotational stiffness; φ_j : rotation; U_j : utilization of the connection; tolerances of equilibrium 1 kN / 1 kNm

*) maximum utilization

maximum utilization [Lk 4]: $\max U = 0.996 < 1$ ok

verification succeeded

3. Detailed edition of Lk 1

notes

no verification for welds within the connection.

notes

connection is verified due to EC 3-1-8 regardless of preloading.
 however, connections may be constructed with prestressed high strength bolts.
 simplified calculation of shear force resistance takes all bolt-rows into account.
 no consideration of bolt groups in joints with 4 bolts per row.

3.1. design values

slope angle: $\alpha_b = \alpha_v = \alpha = 0^\circ$

internal forces and moments perpendicular to the connection planes

periphery beam

$M_d = 2200.00$ kNm, $V_d = 800.00$ kN

partial internal forces and moments

internal forces and moments in the periphery end-plate-beam: $M'_d = M_d - V_d \cdot t_{ep} = 2160.00$ kNm

$N_{b,t} = -N_d \cdot z_{bu} / z_b + M'_d / z_b = 3195.27$ kN, $z_b = 676.0$ mm, $z_{bu} = 338.0$ mm

$N_{b,c} = N_d \cdot z_{bo} / z_b + M'_d / z_b = 3195.27$ kN, $z_b = 676.0$ mm, $z_{bo} = 338.0$ mm

3.2. resistance of cross-section

plastic cross-sectional check for $M_y = -2160.00$ kNm, $V_z = 800.00$ kN

valid normal/shear stress: zul $\sigma_{Rd} = 23.50$ kN/cm², zul $\tau_{Rd} = 13.57$ kN/cm²

top flange: resistance forces $N_{max,O} = 2857.60$ kN, $N_{min,O} = -2857.60$ kN

bottom flange: resistance forces $N_{max,U} = 2857.60$ kN, $N_{min,U} = -2857.60$ kN

web: shear force $V_S = 800.00$ kN, shear stress $\tau_S = 5.64$ kN/cm² $\Rightarrow U_{\tau,S} = 0.415$

resistance forces $N_{max,S} = 3034.68$ kN, $N_{min,S} = -3034.68$ kN

main bending: moment $M_y = -2160.00$ kNm, resistance moments $M_{y,max} = 2444.60$ kNm, $M_{y,min} = -2444.60$ kNm $\Rightarrow U_{M_y} = 0.884$

total (possibly due to load increase): max $U = 0.892 < 1$ **ok**

utilizations: resistance $U_{\sigma} = 0.892 < 1$ **ok**, c/t-ratio $U_{c/t} = 0.334 < 1$ **ok**

3.3. basic components

3.3.1. Gk 5: end-plate in bending

connections with 4 bolts per bolt-row are not treated in EC 3-1-8.

verification follows the final report of AIF-project 15059.

extended part of end-plate

in projecting part of end plate only one bolt-row ($n_b = 1$) is considered (4 bolts per row).

effective length of the T-stub flange (end-plate):

in mode 1: $\Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 220.0$ mm, $l_{eff,cp} = 473.8$ mm

in mode 2: $\Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 220.0$ mm

tension resistance of the T-stub flange:

in mode 1+2: $M_{pl,Rd} = (0.25 \cdot \Sigma l_{eff} \cdot t^2 \cdot f_y) / \gamma_{M0} = 29.56$ kNm

in mode 3: $\Sigma F_{t,Rd} = 4 \cdot n_b \cdot F_{t,Rd} = 2352.96$ kN

mode 1: complete yielding of the T-stub flange

$F_{T,1,Rd} = ((8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 2560.80$ kN

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$F_{T,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 1756.36$ kN

mode 3: bolt failure

$F_{T,3,Rd} = \Sigma F_{t,Rd} = 2352.96$ kN

tension resistance of the T-stub flange: $F_{T,Rd} = \min(F_{T,1,Rd}, F_{T,2,Rd}, F_{T,3,Rd}) = 1756.36$ kN

resistance of a weld (req.1): $f_{1w,d} = f_u / (\beta_w \cdot \gamma_{M2}) = 360.0$ N/mm²

tension resistance of welds: $F_{T,w,Rd} = 2^{1/2} \cdot f_{1w,d} \cdot a \cdot l_{eff} = 2128.11$ kN (≥ 1756.36 kN, not decisive)

resistance and effective length of end-plate in bending (projection)

$F_{t,ep,Rd,1} = 1756.36$ kN, $l_{eff,1} = 220.0$ mm

part of end-plate between beam flanges

equivalent T-stub flange (each individual bolt-row):

here: number of bolt-rows $n_b = 1$

ROW 2 (4 bolts per row)

effective length of the T-stub flange (end-plate):

in mode 1: $\Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 416.8$ mm, $l_{eff,cp} = 668.4$ mm

in mode 2: $\Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 416.8$ mm

tension resistance of the T-stub flange:

in mode 1+2: $M_{pl,Rd} = (0.25 \cdot \Sigma l_{eff} \cdot t^2 \cdot f_y) / \gamma_{M0} = 56.01$ kNm

in mode 3: $\Sigma F_{t,Rd} = 4 \cdot n_b \cdot F_{t,Rd} = 2352.96$ kN

mode 1: complete yielding of the T-stub flange

$F_{T,1,Rd} = ((8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 5493.02$ kN

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$F_{T,2,p,Rd} = (2 \cdot M_{pl,2,Rd} + 0.5 \cdot \Sigma F_{t,Rd} \cdot (n_1^2 + 2 \cdot n_2^2 + 2 \cdot n_1 \cdot n_2) / (n_1 + n_2)) / (m + n_1 + n_2) = 1528.31$ kN

$F_{T,2,np,Rd} = (2 \cdot M_{pl,1,Rd} + 0.5 \cdot \Sigma F_{t,Rd} \cdot n_1) / (m + n_1) = 1510.13$ kN

$F_{T,2,Rd} = \min(F_{T,2,p,Rd}, F_{T,2,np,Rd}) = 1510.13$ kN

mode 3: bolt failure

$F_{T,3,Rd} = 0.9 \cdot \Sigma F_{t,Rd} = 2117.66$ kN

tension resistance of the T-stub flange: $F_{T,Rd} = \min(F_{T,1,Rd}, F_{T,2,Rd}, F_{T,3,Rd}) = 1510.13$ kN

resistance of a weld (req.1): $f_{1w,d} = f_u / (\beta_w \cdot \gamma_{M2}) = 360.0$ N/mm²

tension resistance of welds: $F_{T,w,Rd} = 2^{1/2} \cdot f_{1w,d} \cdot a \cdot l_{eff} = 2122.01$ kN (≥ 1510.13 kN, not decisive)

ROW 3 (2 bolts per row)

effective length of the T-stub flange (end-plate):

in mode 1: $\Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 334.2$ mm, $l_{eff,cp} = 334.2$ mm

in mode 2: $\Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 418.4$ mm

tension resistance of the T-stub flange:

in mode 1: $M_{pl,1,Rd} = (0.25 \cdot \Sigma l_{eff,1} \cdot t^2 \cdot f_y) / \gamma_{M0} = 44.91$ kNm

in mode 2: $M_{pl,2,Rd} = (0.25 \cdot \Sigma l_{eff,2} \cdot t^2 \cdot f_y) / \gamma_{M0} = 56.22$ kNm

in mode 3: $\Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 1176.48$ kN

mode 1: complete yielding of the T-stub flange

$F_{T,1,Rd} = ((8 \cdot n - 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 4394.70$ kN

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$F_{T,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 1593.16$ kN

mode 3: bolt failure

$F_{T,3,Rd} = \Sigma F_{t,Rd} = 1176.48$ kN

tension resistance of the T-stub flange: $F_{T,Rd} = \min(F_{T,1,Rd}, F_{T,2,Rd}, F_{T,3,Rd}) = 1176.48 \text{ kN}$

resistance of a weld (req.1): $f_{1w,d} = f_u / (\beta_w \cdot \gamma_{M2}) = 360.0 \text{ N/mm}^2$

tension resistance of welds: $F_{T,w,Rd} = 2^{1/2} \cdot f_{1w,d} \cdot a \cdot l_{eff} = 1701.36 \text{ kN}$ ($\geq 1176.48 \text{ kN}$, not decisive)

resistances and effective lengths of end-plate in bending (per bolt-row):

$F_{ep,Rd,2} = 1510.13 \text{ kN}$, $l_{eff,2} = 416.8 \text{ mm}$

$F_{ep,Rd,3} = 1176.48 \text{ kN}$, $l_{eff,3} = 334.2 \text{ mm}$

3.3.2. Gk 7: beam flange and web in compression

flange bottom: section class for $c/(\varepsilon \cdot t) = 2.86$: 1

web: section class for $\alpha = 0.50$ and $c/(\varepsilon \cdot t) = 27.71$: 1

section class of beam: 1

taking into account the moment-shear force-interaction $V_{Ed} = 800.0 \text{ kN}$

stress due to bending with shear force: $V_{Ed} = 800.0 \text{ kN} \leq 1152.0 \text{ kN} = V_{pl,Rd}/2 \Rightarrow$ no effect

resistance $M_{c,Rd} = M_{pl,Rd} = (W_{pl} \cdot f_y) / \gamma_{M0} = 2476.67 \text{ kNm}$, $W_{pl} = 10539.00 \text{ cm}^3$

resistance of a flange (and web) with compression

$F_{c,f,Rd} = M_{c,Rd} / (h - t_f) = 3663.71 \text{ kN}$

resistance of upper beam flange:

stress due to bending with shear force: $V_{Ed} = 800.0 \text{ kN} \leq 1152.0 \text{ kN} = V_{pl,Rd}/2 \Rightarrow$ no effect

resistance $M_{c,Rd} = M_{pl,Rd} = (W_{pl} \cdot f_y) / \gamma_{M0} = 2476.67 \text{ kNm}$, $W_{pl} = 10539.00 \text{ cm}^3$

resistance of a flange (and web) with compression

$F_{c,f,Rd} = M_{c,Rd} / (h - t_f) = 3663.71 \text{ kN}$

3.3.3. Gk 8: beam web in tension

each individual bolt-row:

row 2

effective width $b_{eff,t,wb} = 416.8 \text{ mm}$ (l_{eff} from bc 5)

resistance of a beam web in tension

$F_{t,wb,Rd} = b_{eff,t,wb} \cdot t_{wb} \cdot f_{y,wb} / \gamma_{M0} = 2056.9 \text{ kN}$

row 3

effective width $b_{eff,t,wb} = 334.2 \text{ mm}$ (l_{eff} from bc 5)

resistance of a beam web in tension

$F_{t,wb,Rd} = b_{eff,t,wb} \cdot t_{wb} \cdot f_{y,wb} / \gamma_{M0} = 1649.2 \text{ kN}$

3.3.4. Gk 10: bolts in tension

tension resistance of one bolt $F_{t,Rd} = (k_2 \cdot f_{ub} \cdot A_s) / \gamma_{M2} = 588.24 \text{ kN}$, $k_2 = 0.90$

punching shear load capacity $B_{p,Rd} = (0.6 \cdot \pi \cdot d_m \cdot t_p \cdot f_{u}) / \gamma_{M2} = 1716.00 \text{ kN}$, $t_p = 50.0 \text{ mm}$

tension-/punching shear load capacity for 4 bolts: $\Sigma F_{tp,Rd} = 4 \cdot \min(F_{t,Rd}, B_{p,Rd}) = 2352.96 \text{ kN}$

row (shear): $\Sigma F_{tp,Rd,1} = 1176.5 \text{ kN}$, $\Sigma F_{tp,Rd,2} = 1176.5 \text{ kN}$, $\Sigma F_{tp,Rd,3} = 1176.5 \text{ kN}$

row (bending): $\Sigma F_{tp,Rd,1} = 2353.0 \text{ kN}$, $\Sigma F_{tp,Rd,2} = 2353.0 \text{ kN}$, $\Sigma F_{tp,Rd,3} = 1176.5 \text{ kN}$

3.3.5. Gk 11: bolts in shear

shear resistance per shear plane $F_{v,Rd} = \alpha_v \cdot f_{ub} \cdot A / \gamma_{M2} = 488.58 \text{ kN}$, $\alpha_v = 0.60$

shear resistance of 4 bolts (1-shear): $\Sigma F_{v,Rd} = 4 \cdot F_{v,Rd} = 1954.32 \text{ kN}$

row: $\Sigma F_{v,Rd,1} = 977.2 \text{ kN}$, $\Sigma F_{v,Rd,2} = 977.2 \text{ kN}$, $\Sigma F_{v,Rd,3} = 977.2 \text{ kN}$

3.3.6. Gk 12: plate with bearing resistance

row 1

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 568.33 \text{ kN}$, $k_1 = 1.71$, $\alpha_b = 0.64$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 568.33 \text{ kN}$, $k_1 = 1.71$, $\alpha_b = 0.64$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 1136.66 \text{ kN}$

row 2

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 886.60 \text{ kN}$, $k_1 = 1.71$, $\alpha_b = 1.00$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 886.60 \text{ kN}$, $k_1 = 1.71$, $\alpha_b = 1.00$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 1773.19 \text{ kN}$

row 3

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 886.60 \text{ kN}$, $k_1 = 1.71$, $\alpha_b = 1.00$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 886.60 \text{ kN}$, $k_1 = 1.71$, $\alpha_b = 1.00$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 1773.19 \text{ kN}$

bearing resistance (3 rows)

$\Sigma F_{b,Rd,1} = 1136.66 \text{ kN}$

$\Sigma F_{b,Rd,2} = 1773.19 \text{ kN}$

$\Sigma F_{b,Rd,3} = 1773.19 \text{ kN}$

3.4. connection capacity

3.4.1. moment resistance

distance of tension-bolt-rows from centre of compression: $h_1 = 776.0$ mm, $h_2 = 576.0$ mm, $h_3 = 101.0$ mm

resistance per bolt-row (MNV-interaction)

row 1: $F_{tr,Rd} = 1756.4$ kN

row 2: $F_{tr,Rd} = 1510.1$ kN

row 3: $F_{tr,Rd} = 397.2$ kN

resistance of flanges (MNV-interaction)

bottom: $F_{c,Rd} = 3663.7$ kN

moment resistance (MNV-interaction)

$M_{j,Rd} = \Sigma(F_{tr,Rd} \cdot h_r) = 2272.9$ kNm

shear force resistance (MNV-interaction)

$V_{j,Rd} = 826.5$ kN

3.4.2. shear resistance

shear resistance of end plate

end-plate: $V_{ep,Rd} = 3612.19$ kN

welds: $F_{w,Rd} = 2419.33$ kN

shear resistance of end plate: $V_{ep,Rd} = F_{w,Rd} = 2419.33$ kN

3.5. verifications

3.5.1. verification of the connection capacity by means of the component method

$U_{MNV} = 0.968 < 1$ ok

$V_{Ed}/V_{ep,Rd} = 0.331 < 1$ ok

3.5.2. verification result

maximum utilization: $\max U = 0.968 < 1$ ok

3.6. rotational stiffness

stiffness coefficients

equivalent stiffness coefficient for 3 tension-bolt-rows:

1: $k_5 = 123.60$ mm, $k_{10} = 9.49$ mm $\Rightarrow k_{eff,1} = 1 / \Sigma(1/k_{i,1}) = 14.520$ mm

2: $k_5 = 311.66$ mm, $k_{10} = 9.49$ mm $\Rightarrow k_{eff,2} = 1 / \Sigma(1/k_{i,2}) = 16.919$ mm

3: $k_5 = 249.88$ mm, $k_{10} = 9.49$ mm $\Rightarrow k_{eff,3} = 1 / \Sigma(1/k_{i,3}) = 8.820$ mm

$k_{eq} = \Sigma(k_{eff,r} \cdot h_r) / z_{eq} = 33.209$ mm, $z_{eq} = \Sigma(k_{eff,r} \cdot h_r^2) / \Sigma(k_{eff,r} \cdot h_r) = 659.6$ mm

rotational stiffness

initial rotational stiffness: $S_{j,ini} = (E \cdot z^2) / \Sigma(1/k_i) = 3033835.4$ kNm/rad, $z = z_{eq} = 659.6$ mm, $\Sigma(1/k_i) = 0.030$ mm⁻¹

rotational stiffness: $S_{j,Rd} = S_{j,ini} / \mu = 3033835.4$ kNm/rad, $\mu = 1$

rotation: $\varphi_{j,Ed} = M_{j,Ed} / S_{j,Rd} = 0.042^\circ$